

1) Determine whether each point lies on the line represented by the parametric equation:

$$x = -2 + t, y = 3t, z = 4 + t$$

a) $(0, 6, 6)$ Yes

b) $(2, 3, 5)$ No

2) Determine whether each point lies on the line represented by the symmetric equation: $\frac{x-3}{2} = \frac{y-7}{8} = z+2$

a) $(7, 23, 0)$ Yes

b) $(1, -1, -3)$ Yes

3) A line passes through the points $(0, 4, 3)$ and $(-1, 2, 5)$, find the following (write the direction number as integers):

a) Parametric equations of the line.

b) Symmetric equations of the line.

a) $x = t, y = 4 + 2t, z = 3 - 2t$

b) $x = \frac{y-4}{2} = \frac{z-3}{-2}$

4) Find a set of parametric equations of the following lines:

a) The line that passes through the point $(2, 3, 4)$ and is parallel to the xz -plane and the yz -plane.

b) The line that passes through the point $(2, 3, 4)$ and is perpendicular to the plane given by $3x + 2y - z = 6$

c) The line that passes through the point $(5, -3, -4)$ and is parallel to $\vec{v} = \langle 2, -1, 3 \rangle$.

d) The line that passes through the point $(2, 1, 2)$ and is parallel to the line: $x = -t, y = 1 + t, z = -2 + t$

a) $x = 2, y = 3, z = 4 + t$

b) $x = 2 + 3t, y = 3 + 2t, z = 4 - t$

c) $x = 5 + 2t, y = -3 - t, z = -4 + 3t$

d) $x = 2 - t, y = 1 + t, z = 2 + t$

5) Determine which of the following lines are parallel and which once are identical.

$$L_1: x = 6 - 3t, y = -2 + 2t, z = 5 + 4t$$

$$L_2: x = 6t, y = 2 - 4t, z = 13 - 8t$$

$$L_3: x = 10 - 6t, y = 3 + 4t, z = 7 + 8t$$

$$L_4: x = -4 + 6t, y = 3 + 4t, z = 5 - 6t$$

L_1 and L_2 are identical. L_1 and L_2 are parallel to L_3

6) Determine the point where the lines intersect and the cosine of the angle of intersection.

$$x = 4t + 2, y = 3, z = -t + 1$$

$$x = 2s + 2, y = 2s + 3, z = s + 1$$

$$(2, 3, 1), \cos \theta = \frac{7\sqrt{17}}{51}$$

7) Determine whether the plane $x + 2y - 4z - 1 = 0$ passes through each point.

a) $(-7, 2, -1)$ Yes

b) $(5, 2, 2)$ Yes

8) Find an equation of the plane:

- The plane passes through $(3, -1, 2)$, $(2, 1, 5)$, and $(1, -2, -2)$.
- The plane passes through the point $(1, 2, 3)$ and is parallel to yz -plane.
- The plane contains the lines given by: $\frac{x-1}{-2} = y-4 = z$ and $\frac{x-2}{-3} = \frac{y-1}{4} = \frac{z-2}{-1}$
- The plane passes through the point $(2, 2, 1)$ and contains the line given by: $\frac{x}{2} = \frac{y-4}{-1} = z$
- The plane passes through the points $(2, 2, 1)$ and $(-1, 1, -1)$ and is perpendicular to the plane $2x - 3y + z = 3$.
- The plane passes through the points $(4, 2, 1)$ and $(-3, 5, 7)$ and is parallel to the z -axis.

- $x + 2y - z + 1 = 0$
- $x = 1$
- $x + y + z = 5$
- $x - 2z = 0$
- $7x + y - 11z = 5$
- $3x + 7y = 26$

9) Find the points where the line $x = 1 - 2t$, $y = -1 + 3t$, $z = -4 + t$ intersects the xy , xz and yz -planes.

$$\left(-7, 10, 0 \right), \left(-\frac{1}{3}, 0, -\frac{10}{3} \right), \left(0, -\frac{1}{2}, -\frac{7}{2} \right)$$

10) Find an equation of the plane that contains all the points that are equidistant from the points: $(2, 2, 0)$ and $(0, 2, 2)$

$$x - z = 0$$

11) Determine whether the planes are parallel, orthogonal or intersect. If they intersect find the angle of intersection.

$$x - 3y + 6z = 4$$

$$5x + y - z = 4$$

Intersect, $\theta \approx 83.5^\circ$

12) Find the x , y and z intercepts of the plane $4x + 2y + 6z = 12$.

$(3, 0, 0), (0, 6, 0), (0, 0, 2)$

13) Find a set of parametric equations for the line of intersection of the planes:

$$3x + 2y - z = 7$$

$$x - 4y + 2z = 0$$

$x = 2, y = 1 + t, z = 1 + 2t$

14) Find the point(s) of the intersection (if any) of the plane $2x - 2y + z = 12$ and the line $x - \frac{1}{2} = \frac{y + (3/2)}{-1} = \frac{z + 1}{2}$.

Also determine whether the line lies in the plane.

$(2, -3, 2)$, The line does not lie in the plane.

15) Find the distance between the point $(2, 8, 4)$ and the plane $2x + y + z = 5$.

$$\frac{11\sqrt{6}}{6}$$

16) Verify that the two planes are parallel, and find the distance between the planes.

$$x - 3y + 4z = 10$$

$$x - 3y + 4z = 6$$

$$\frac{2\sqrt{26}}{13}$$

17) Find the distance between the point $(1, -2, 4)$ and the line $x = 2t$, $y = t - 3$, $z = 2t + 2$.

$$\frac{\sqrt{5}}{3}$$

18) Verify that the lines are parallel, and find the distance between them:

$$L_1 : x = 2 - t, \quad y = 3 + 2t, \quad z = 4 + t$$

$$L_2 : x = 3t, \quad y = 1 - 6t, \quad z = 4 - 3t$$

$$\frac{\sqrt{66}}{3}$$

19) Find the distance between the skew lines:

$$x = 1 + t, \quad y = 1 + 6t, \quad z = 2t$$

$$x = 1 + 2s, \quad y = 5 + 15s, \quad z = -2 + 6s$$

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20) Find the standard equation of the sphere with center $(-3, 2, 4)$ that is tangent to the plane given by $2x + 4y - 3z = 8$.

$$\boxed{(x + 3)^2 + (y - 2)^2 + (z - 4)^2 = \frac{324}{29}}$$